About this booklet...

Welcome to the world of **CASIO** scientific calculator. In this booklet, you will find some Mathematics problems of lower secondary till upper secondary level, which were carefully selected to demonstrate the use of the **CASIO** *fx*-570MS scientific calculator. The examples presented are among those commonly encountered while teaching and learning Mathematics in the lower and upper secondary in Malaysia.

You will probably know by now that the calculator is a tool that could speed up calculations efficiently and thus allows you to spend more time in understanding theory and logic of Mathematics.

It is important to remember that this booklet is not meant to replace the User's Guide that comes with your CASIO fx-570MS pack. Do read the User's Guide carefully before using this booklet.

We sincerely hope that you will enjoy working through the worked examples provided in this booklet. Having understood the usage of your CASIO fx-570MS scientific calculator, may it serve you more efficiently and effectively!

About the Author...

QED Education Scientific works to provide many wonderful resources and support to teachers & students using **CASIO** scientific calculator. With support from **Marco Corporation**, the sole distributor of **CASIO** range of calculators and the publisher of this booklet, we have been producing supplementary booklets, training manuals, training presentations and comprehensive professional development programme for in-service teachers using **CASIO** classroom technology for the past 3 years. The training arm of the consultancy was involved in the Curriculum Development Centre's *Graphics Calculator for Mathematics and Science* project in 2003.

About the Editor...

Nellie Gan Hong Suan obtained her Bachelor degree (Mathematics-Economics) from *Universiti Malaya* and her Master degree (Management Science) from *Universiti Utara Malaysia*. She has eighteen years of experience teaching Mathematics. She has also been involved in writing workbooks and reference books for secondary Mathematics. She is currently a Mathematics lecturer in *Maktab Perguruan Teknik*, Kuala Lumpur.

INTRODUCTION

Purpose of This Booklet...

This booklet is not intended to replace the *fx*-570MS User's Guide, nor any mathematics reference book. It is written with the aim that users of the powerful *fx*-570MS calculator, especially students, can acquire what we called "calculator skills". These skills will not be tested in any public examinations. However, we believe having developed these skills, students' interest in studying mathematics will be further enhanced. We believe they would have more fun exploring and investigating new mathematical ideas and concepts, and we wish to see in future students *enjoy* doing mathematics and tackling challenging mathematical problems.

This booklet is also to serve as an extension to our previous work on the equally interesting CASIO *fx*-350MS scientific calculator, *Exploring Mathematics with CASIO fx*-350MS.

Working With This Booklet...

The booklet is written with the assumption that the user has sufficient secondary mathematics training. As it is designed for Form 1 to Form 6 students, worked-examples in this booklet are selected problems from some topics in PMR's Mathematics, SPM's Mathematics and Additional Mathematics, and STPM Mathematics. *Appendix 1* is a list of *English* ~ *Bahasa Malaysia* mathematical terminologies used throughout the booklet.

We will be glad to entertain any feedbacks from the readers on this booklet. We love to hear from you at info@qed-edu.com

Support For the Reader...

To capture the essence of mathematics requires one to spend time in improving and reinforcing the fundamental principles by working through exercises provided in textbooks and reference books. May this booklet and the wonderful fx-570MS calculator help you in achieving this.

If you want to know more about this model, please visit these sites:

- CASIO Education site: www.casio.co.jp/edu e
- Marco Corporation site: www.marco-groups.com

Other related resources on *fx*-570MS available are:

- The Enjoyable Path to Math: A supplementary reader.
- Exploring Mathematics with CASIO fx-350MS.

Or email to us at info@qed-edu.com.

TABLE OF CONTENTS

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Page

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◆ Let's Get St@rted!	1
♦ Simultaneous Linear Equations	7
♦ Surface Area and Volume of Solid	8
♦ Statistic I	9
♦ Number Systems	11
◆ Quadratic and Cubic Equations	12
♦ Differential: A Numerical Approach	14
◆ Definite Integral: Area of Region	15
♦ Statistics II	16
♦ Matrices: 2×2 and 3×3	17
♦ Complex Numbers	20
Appendix 1	21

→ Let's Get St@rted! →

There are two things you need to know before we start:

To activate any function in yellow, precede it by pressing the SHIFT *key. To activate any function in red, precede it by pressing the* ALPHA *key.*

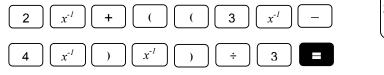
Now, let's try them out!

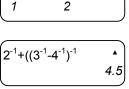
Example 1 Evaluate
$$\frac{1}{2} + \left(\frac{1}{\frac{1}{3} - \frac{1}{4}}\right) \div 3$$
, then express it as an improper fraction.

OPERATION

1. Choose COMP mode.

2. Key in the expression and evaluate.





CMPLX

COMP

3. Expressing the outcome as an improper fraction.



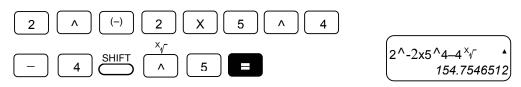
2 ⁻¹ +((3 ⁻¹ -4 ⁻¹) ⁻¹	•
	9 _2.

Which is greater, (a) $2^{-2} \times 5^4 - \sqrt[4]{5}$ or (b) $2^{-2} \times (5^4 - \sqrt[4]{5})$?

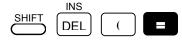
OPERATION

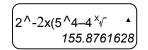
Example 2

1. While in COMP mode, press the following to evaluate $2^{-2} \times 5^4 - \sqrt[4]{5}$.



2. To calculate $2^{-2} \times (5^4 - \sqrt[4]{5})$, use the INS function to insert the bracket. Press numerous times until the cursor is below "5", then press





Obviously, (b) $2^{-2} \times (5^4 - \sqrt[4]{5})$ is greater than (a) $2^{-2} \times 5^4 - \sqrt[4]{5}$.

Example 3

Evaluate $9.2 \times 10^5 - 4.3 \times 10^3$.

OPERATION

1. Choose COMP mode, then evaluate $9.2 \times 10^5 - 4.3 \times 10^3$.



Therefore, $9.2 \times 10^5 - 4.3 \times 10^3$ is equal to 915 700.

Example 4

Find value of x which satisfies $(\ln 4)^x = 5$.

OPERATION

1. To solve this example for x we calculate $x = \frac{\ln 5}{\ln(\ln 4)}$, since $\ln(\ln 4)^x = \ln 5$



In 5÷ln (In4 ▲ 4.927339565

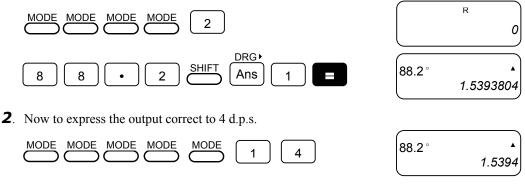
The solution is thus approximately 4.93.

Example 5

Convert 88.2° to its radian equivalent, correct to 4 d.p.s.

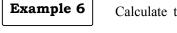
OPERATION

1. First enter Rad mode, then key in 88.2° to perform the conversion.



The above conversion shows that $88.2^{\circ} = 1.5394 rad$, correct to 4 d.p.s.

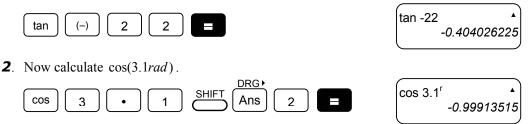




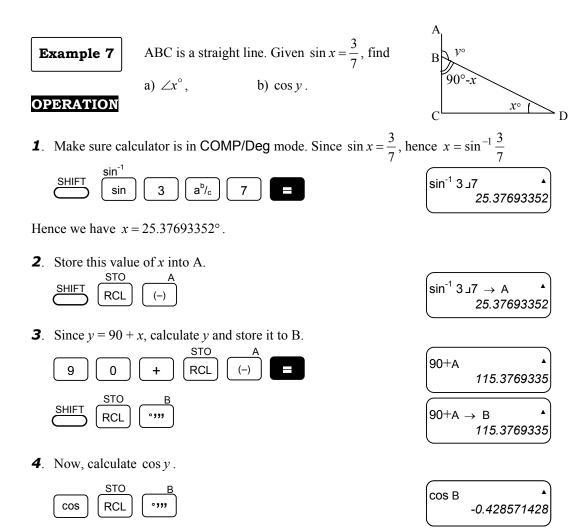
Calculate $tan(-22^{\circ})$ and cos(3.1rad).

OPERATION

1. While you are in COMP/Deg (degree) mode, key in $tan(-22^{\circ})$.



Hence, $tan(-22^{\circ})$ and cos(3.1rad) are approximately -0.4040 and -0.9991 respectively.

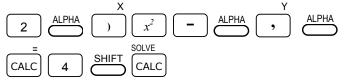


Hence, $\cos y$ is approximately -0.429.

Example 8 Given that $2x^2 - y = 4$ and x = 3, find y.

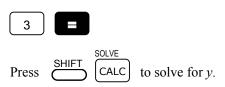
OPERATION

1. While you are in COMP mode, enter the equation follow by the SOLVE function.





2. Now the displayed screen requests for the value of *x*.



Y?	•
	0
Y?	
	14

Hence, y = 14.

Example 9

- (a) A class of 30 students wants to have a class monitor, an assistant monitor & a treasurer. In how many ways can such a committee be formed?
- (b) A group of 4 students is to be chosen from a class of 28 for a debate team. In how many ways can such a group be formed?

OPERATION

1. This is essentially the permutation of 30 objects taken 3 at a time.

nPr	
3 0 SHIFT X	3



Hence, there are 24 360 ways to form the class committee.

2. While (b) is the combinations of 28 objects taken 4 at any time.



28C4 ***** 20475

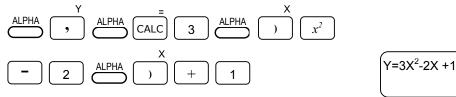
This means that the number of combinations is 20 475.

Example 10

Given that $y = 3x^2 - 2x + 1$ where $-2 \le x \le 2$, $x \in \mathbb{Z}$. Find the corresponding values of y and construct a table of values.

OPERATION

1. Press the following to key in the function.



2. Input the first *x* value, x = -2.





This means y = 17 when x = -2.

3. Input the next x value, x = -1.



 $\begin{pmatrix} Y=3X^2-2X+1 & \bullet \\ & & 6 \end{pmatrix}$

 $Y=3X^{2}-2X+1$

Х?

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0

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0

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17

This means y = 6 when x = -1.

4. Continue replacing x = 0, 1, 2, and values obtained for y are 1, 2, 9 respectively.

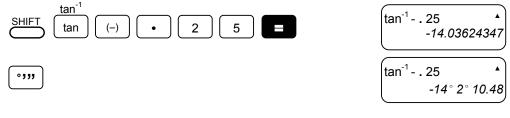
x	-2	-1	0	1	2
У	17	6	1	2	9



Given that $\tan x = -0.25$, where $270 \le x \le 360^{\circ}$. Find value of x that satisfies the equation.

OPERATION

1. Choose COMP mode. To find the basic acute angle α , we use $\alpha = \tan^{-1} 0.25$,



2. Since *x* lies in the fourth quadrant.



Hence, x is approximately $345^{\circ}58'$.

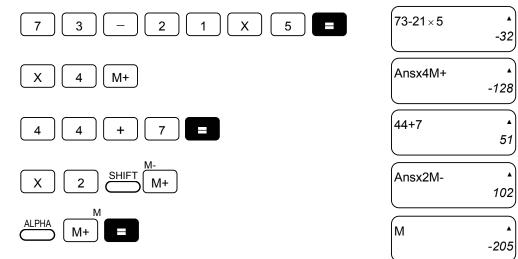
```
Example 12 Calculate (53-28) + 4[73-(21\times 5)] - 2(44+7).
```

OPERATION

1. While in COMP mode, key in the expression for calculation. Then store the output to M.

STO		$\overline{}$
SHIFT DOL MA	53-28 → M	•
		25
)

2. Calculate the other expressions and use the function M+ to store the output.



Hence, $(53-28) + 4[73-(21\times5)] - 2(44+7) = -205$.

→ Simultaneous Linear Equations →

Example 1

Solve the following linear equations simultaneously.

0.5x + 3.7y = 23x - 11y = -3

OPERATION

1. Press the MODE key until you see the screen at right.

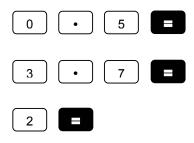


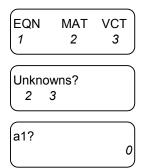
Select EQN by tapping 1 once.

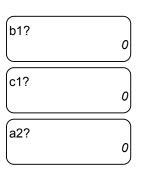
As this is a problem of 2 unknowns, we choose 2.



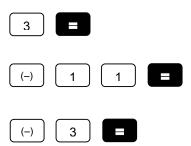
2. Now key in the coefficients and constant of the first equation.





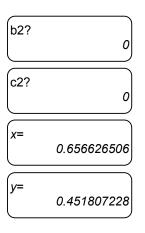


3. And the coefficients and constant of the second equation.



Press ∇ to view the solution for *y*.

Hence the solution is x = 0.657, y = 0.452, correct to 3 d.p.s.



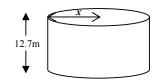
→ Surface Area and Volume of Solid →

Example 1

A closed cylindrical water tank is such that the height of the tank is 12.7m and its radius varies between 15m and 39.6m inclusive. Find the amount of material needed to produce this tank

when its radius is

(i) maximum, (ii) twice its height.



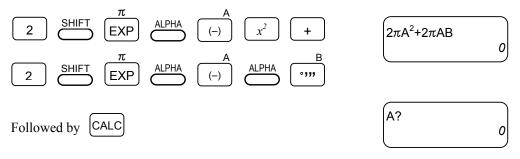
OPERATION

1. First enter COMP mode.

MODE	\square
\square	



2. Calculate the tank surface area using the cylindrical formula, $2\pi r^2 + 2\pi rh$. We shall let A, B represent *r*, *h* respectively, and use the CALC function.

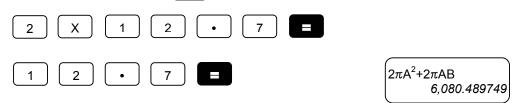


3. Input the values A=39.6 and B=12.7 to calculate part (i).



Therefore, the amount of material needed when radius is maximum, or when A=39.6, is approximately $13012.98m^2$.

4. To calculate part (ii), press CALC immediately after and input $A=2\times12.7$ and B=12.7.



Hence approximately 6080.49m² of material is needed when the tank's radius is twice its height.

→ Statistic I →

Example 1

Below are weights distribution of 20 students in a class.

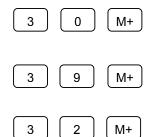
30	39	34	37	39	31	32	33	32	30
32	35	38	41	35	35	37	39	35	39

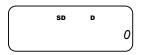
Find the mean of the distribution.

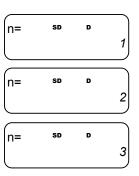
OPERATION

1. Enter SD (standard deviation) mode.

2. Now key in all data.









3. To obtain the mean, press

9

3



• (continue keying in the rest of the data)

M+

35.15

 \overline{x}

Therefore we have obtained the mean of the distribution as 35.15.

► Statistic I

Example 2

Table below shows the quantity of drinks (in litre) bought by 70 students during a sport event.

In litre	1	2	3	4	5	6
No of Students	9	14	22	12	9	4

Find the mean & the standard deviation of quantity of drinks bought.

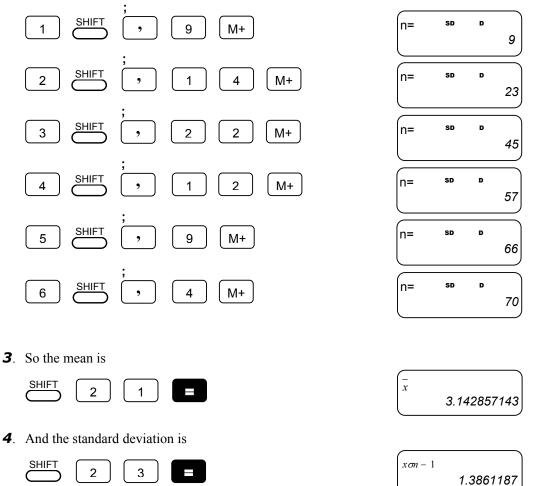
OPERATION

1. First enter SD (standard deviation) mode.

MODE	MODE	
\bigcirc	\bigcirc	

SD D 0

2. Then key in all data.



Therefore, the mean and standard deviation of drinks bought by the 70 students are approximately 3.14 & 1.39 respectively.

→ Number Systems →

Example 1

(a) Express 22_8 in decimal (base 10).

(b) Calculate $28_{10} \times 111_2 + 35_{10}$. Leave your answer in binary.

OPERATION

1. First enter BASE mode. (Your display screen maybe different.)





22

2. Now key in 22_8 .



3. Convert 22_8 into its base 10 equivalent.

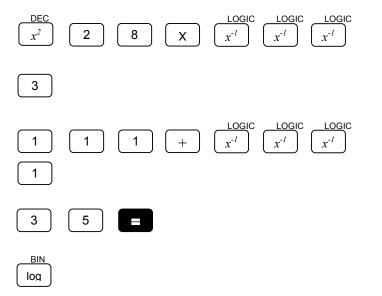


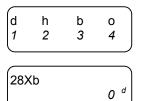
22		
22	18	d

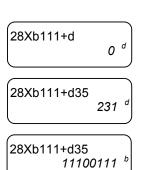
22

Therefore 22_8 , which is in octal (base 8), is equivalent to 18_{10} .

4. Now to calculate (b) $28_{10} \times 111_2 + 35_{10}$.

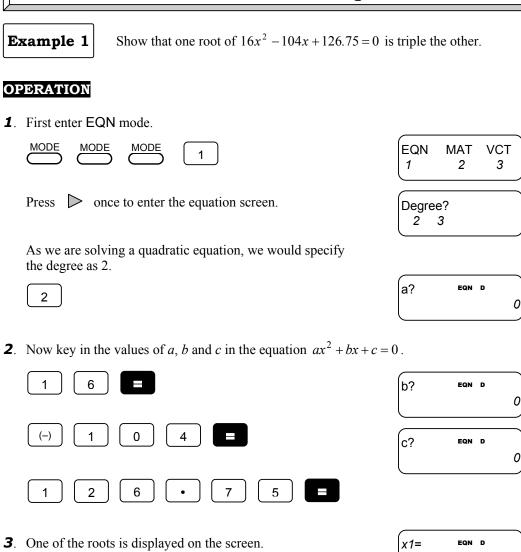






Hence, $28_{10} \times 111_2 + 35_{10}$ is equivalent to 11100111_2 .

→ Quadratic and Cubic Equations →



Press ∇ to view the other root.

Obviously the root 4.875 is triple the other root, 1.625, as $4.875 = 3 \times 1.625$.

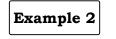
4.875

1.625

EQN D

x2=

► Quadratic and Cubic Equations

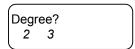


Solve the cubic equation of $x^3 - 9x^2 + 19x + 29 = 0$ for x.

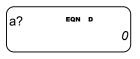
OPERATION

1. First enter EQN mode, then enter the equation screen.

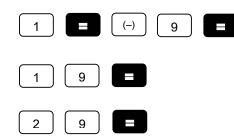
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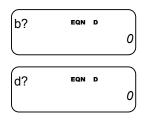


As we are solving a cubic equation, specify the degree as 3.



2. Input the values of *a*, *b*, *c* and *d* for the equation $ax^3 + bx^2 + cx + d = 0$.





3 .	The first solution is displayed.	x1=	EQN D	
	Press ∇ to view other solutions.			-1
	The symbol $R \leftrightarrow I$ at the upper right means that the solution displayed is a complex number, and its real part is 5. To display its imaginary part, press	x2=	EQN D	^{R⇔I} 5
	SHIFT	x2=	EQN D	_{R⇔I} 2 _i

Each press of **SHIFT Re**↔**Im** toggles the display between the real part and imaginary part.

4. Tap ∇ to view the final solution, which is also a complex number.



Therefore the solutions to $x^3 - 9x^2 + 19x + 29 = 0$ are x = -1, x = 5 + 2i and x = 5 - 2i, where the two complex solution are conjugates of each other.

Differential: A Numerical Approach

Example 1

Show that 2 of the stationary points of $f(x) = x^3 - 4x^2 - 11x + 30$ are at x = -1 and $x = \frac{11}{3}$.

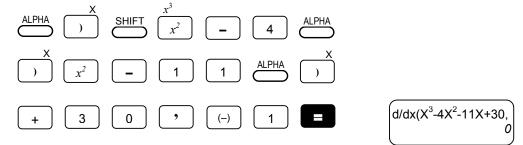
OPERATION

1. While in COMP more, press



d/dx(

2. Key in the function and evaluate f'(-1).



As f'(-1) = 0, one of $f(x) = x^3 - 4x^2 - 11x + 30$ stationary points lies on x = -1.

3. Now to evaluate $f'(\frac{11}{3})$, tap on \triangleleft a few times until the cursor is below the minus sign.

X ³ -4X ² -11X+30,-1_	
	0

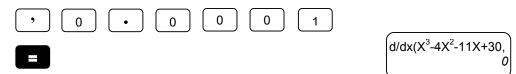
4. Replace -1 with $\frac{11}{3}$.

 $\triangleleft \triangleleft$



 \triangleleft

Let the change in x, Δx as 0.0001. This would improve the numerical method's accuracy.



As with before, since $f'(\frac{11}{3}) = 0$, therefore a stationary point of $f(x) = x^3 - 4x^2 - 11x + 30$ lies on $x = \frac{11}{3}$.

→ Definite Integral: Area of Region →

Example 1

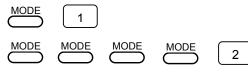
Determine the area of the region bounded by $y = 2 \sin x$, the x-axis,

$$x = 0$$
 and $x = \frac{\pi}{4}$

For this example we divide the region into **Region I** and **Region II** as illustrated in Figure 1.

OPERATION

1. Enter COMP mode and switch to Rad (radian), as the definite integral involves upper and lower bounds in radian.

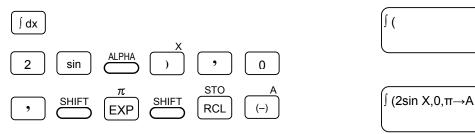




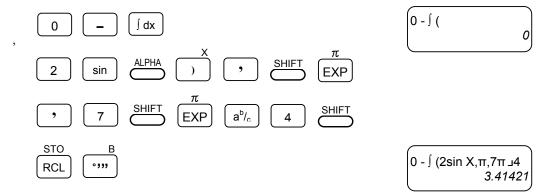
0

4

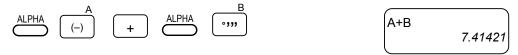
2. Calculate the area of **Region I** and store the answer to A. The calculation may take a few seconds.



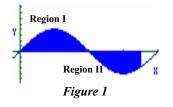
3. Now calculate the area of **Region II** and store the answer to B.



4. The area of the region is equivalent to the sum of values stored in A and B.



Therefore the area of this region is 7.41421 unit².



→ Statistic II →

Find the following standardised normal distribution. (a) P(Z > 0.825), (b) $P(Z \le 1.054)$,

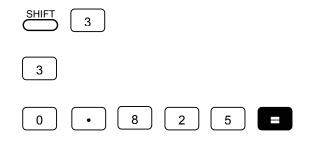
(c) $P(-1.2 \le Z \le 0.3)$.

OPERATION

1. Enter SD (standard deviation) mode.

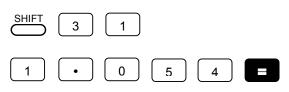


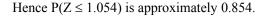
2. First find P(Z > 0.825).



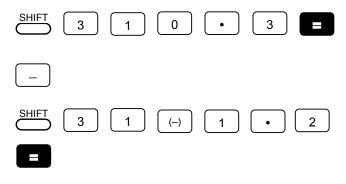
Hence P(Z > 0.825) is approximately 0.205.

3. Next, find $P(Z \le 1.054)$.

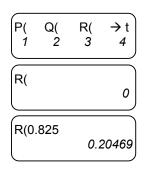


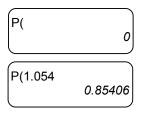


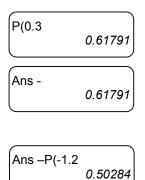
4. Now to obtain $P(-1.2 \le Z \le 0.3)$.



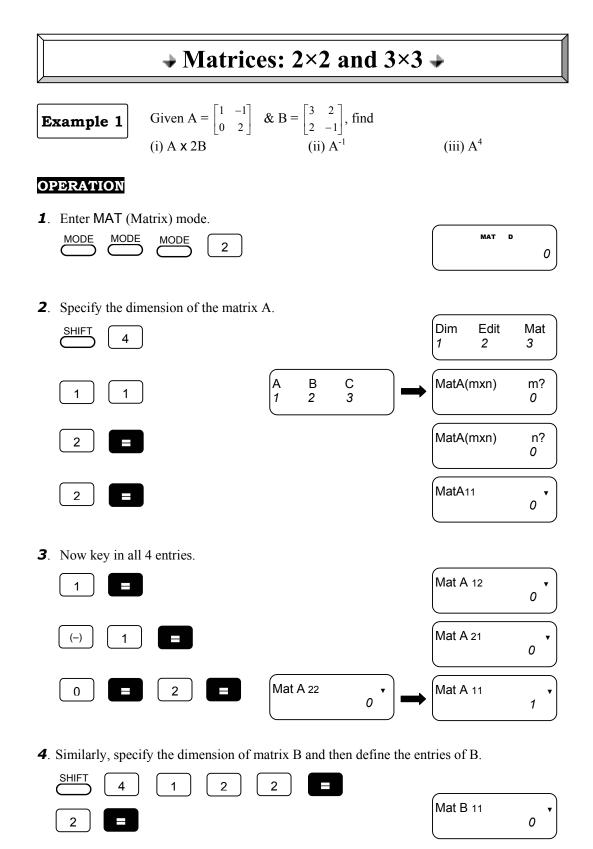
SD D O







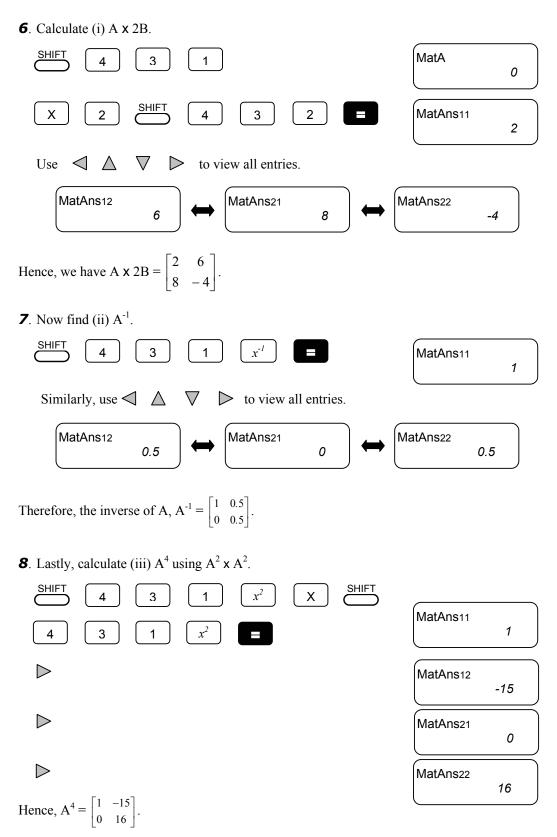
Therefore P (-1.2 \leq Z \leq 0.3) is approximately 0.503.



(–)

Mat B 11

► Matrices:2x2 and 3x3



► Matrices:2x2 and 3x3

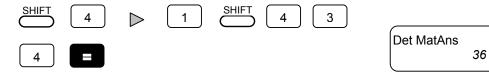


Given $C = \begin{bmatrix} 2 & -1 & 0 \\ 1 & -2 & 0 \\ 0 & 1 & 3 \end{bmatrix} \& D = \begin{bmatrix} 1 & -2 & 0 \\ 0 & 2 & 1 \\ 3 & 0 & 1 \end{bmatrix}$, find determinant of $C \times D^{T}$.

OPERATION

1. While in MAT mode, specify the dimension of the 3x3 matrix C.

$\stackrel{\text{SHIFT}}{\longleftarrow} \begin{bmatrix} 4 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 3 \\ 3 \end{bmatrix} = \begin{bmatrix} 3 \\ 3 \end{bmatrix}$		
	Mat A 11	0
2 . Key in all entries of matrix C.		
3	Mat A 11	2
3 . Similarly, specify the dimension of matrix D and key in its entries.		
SHIFT 4 1 2 3 = 3		
	Mat B 11	1
4 . First we calculate $C \times D^{T}$.		
$ \begin{array}{c} \text{SHIFT} \\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $	MatAns12	-2
Use \triangleleft \triangle ∇ \triangleright to view all entries.	MatAns32	•
Hence, $\mathbf{C} \times \mathbf{D}^{\mathrm{T}} = \begin{bmatrix} 3 & 0 & 9 \\ -6 & 6 & 0 \\ -1 & 11 & 12 \end{bmatrix}$.	L	5
5 . Now to find determinant of $\mathbf{C} \times \mathbf{D}^{\mathrm{T}}$.		



So the determinant of $C \times D^T$ is 36.

→ Complex Numbers →

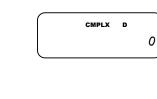
```
Example 1 Give
```

Given that $z_1 = 1 - 3i$ and $z_2 = 2 + 7i$, express $z_1 + z_2$ in polar form.

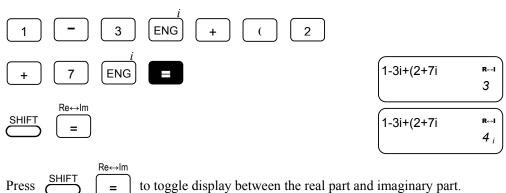
OPERATION

1. First enter CMPLX/Deg mode.

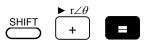




2. Now calculate $z_1 + z_2$.



3. Expressing $z_1 + z_2$ in polar form.



Here the modulus of $z_1 + z_2$ is 5.

SHIFT

53.13010235

5

Ans> r∠θ

Ans> r $\angle \theta$

And the argument is approximately 53.13°

Therefore the complex number $z_1 + z_2$ in polar form is $5 \angle 53.13^{\circ}$

Appendix 1

English ~ Bahasa Malaysia Mathematical Terms

English

Bahasa Malaysia

Acute angle	Sudut tirus
Area	Luas
Bound	Sempadan
Coefficient	Pekali
Combinations	Gabungan
Constant	Pemalar
Cubic	Kubik
Decimal	Perpuluhan
Definite Integral	Kamiran Tentu
Determinant	Penentu
Differential	Pembezaan
Distribution	Taburan
Equation	Persamaan
Expression	Ungkapan
Fraction	Pecahan
Improper fraction	Pecahan tak wajar
Inverse	Songsangan
Mean	Min
Numerical	Berangka
Octal	Perlapanan
Permutations	Pilihatur
Power	Kuasa, eksponen
Probability	Kebarangkalian
Quadrant	Sukuan
Radius	Jejari
Region	Rantau
Roots	Punca-punca
Simultaneous equations	Persamaan serentak
Solution	Penyelesaian
Standard deviation	Sisihan piawai
Stationary point	Titik pegun
Unknown	Anu
Variable	Pembolehubah